## Points of Concurrency

|                                  | Incenter  | Circumcenter   | Centroid  | Orthocenter  |
|----------------------------------|---|--|---|--|
| Formed by<br>intersection<br>of: | Angle Bisectors   | Perpendicular<br>Bisectors   | Medians   | Altitudes  |
| Definition of segments           | At each vertex,<br>bisects angle into two<br>≅ parts.   | Bisects a side into two<br>≅ parts and forms a<br>90° angle.   | Connects a vertex to<br>midpoint of the<br>opposite side.   | Connects a vertex at<br>90° (perpendicular) to<br>opposite side (or<br>extension of).                            |
| Location                         | Always<br>Inside  | <ul> <li>Inside (Acute Δ)</li> <li>ON (Right Δ- at midpoint of hypotenuse)</li> <li>Outside (Obtuse Δ)</li> </ul>              | Always<br>Inside  | <ul> <li>Inside (Acute Δ)</li> <li>ON (Right Δ- at vertex of right angle)</li> <li>Outside (Obtuse Δ)</li> </ul> |
| Segments ARE<br>NOT always       | <ul> <li>passing through<br/>midpoint of<br/>opposite side.</li> <li>perpendicular<br/>(90°) to opposite<br/>side.</li> </ul> | o angle bisectors.   | <ul> <li>angle bisectors.</li> <li>perpendicular<br/>(90°) to opposite<br/>side.</li> </ul>   | <ul> <li>angle bisectors.</li> <li>passing through<br/>midpoint of<br/>opposite side.</li> </ul>                 |
| Special<br>properties:           | <ul> <li>&gt; equidistant from<br/>the sides of the<br/>∆.</li> <li>&gt; center of the<br/>inscribed circle.</li> </ul>       | <ul> <li>&gt; equidistant from<br/>the vertices of<br/>the ∆.</li> <li>&gt; center of<br/>circumscribed<br/>circle.</li> </ul> | <ul> <li>&gt; located <sup>2</sup>/<sub>3</sub> the distance from vertex to side.</li> <li>&gt; 2:1 ratio from vertex.</li> <li>&gt; center of gravity of ∆.</li> </ul> | ≻ NOTHING!   |



| Special ∆s,<br>special<br>properties: | Equilateral $\Delta s$ : All 4 points are located at the <u>same point</u> . |  |  |
|---------------------------------------|--|--|--|
|                                       | Isosceles ∆s: All 4 points are <u>collinear</u> .                            |  |  |