## Points of Concurrency

|  | Incenter | Circumcenter | Centroid | Orthocenter |
| :---: | :---: | :---: | :---: | :---: |
| Formed by intersection of: | Angle Bisectors | Perpendicular Bisectors | Medians | Altitudes |
| Definition of segments | At each vertex, bisects angle into two $\cong$ parts. | Bisects a side into two $\cong$ parts and forms a $90^{\circ}$ angle. | Connects a vertex to midpoint of the opposite side. | Connects a vertex at 90́ (perpendicular) to opposite side (or extension of). |
| Location | Always Inside | - Inside (Acute $\Delta$ ) <br> - ON (Right $\Delta$ - at midpoint of hypotenuse) <br> - Outside (Obtuse $\Delta$ ) | Always Inside | - Inside (Acute $\Delta$ ) <br> - ON (Right $\Delta$ - at vertex of right angle) <br> - Outside (Obtuse $\Delta$ ) |
| Segments ARE NOT always | - passing through midpoint of opposite side. <br> - perpendicular $\left(90^{\circ}\right)$ to opposite side. | - angle bisectors. | - angle bisectors. <br> - perpendicular (90ㅇ) to opposite side. | - angle bisectors. <br> - passing through midpoint of opposite side. |
| Special properties: | equidistant from the sides of the $\Delta$. <br> > center of the inscribed circle. | > equidistant from the vertices of the $\Delta$. <br> $\Rightarrow$ center of circumscribed circle. | located $\frac{2}{3}$ the distance from vertex to side. 2:1 ratio from vertex. <br> > center of gravity of $\Delta$. | > NOTHING! |



Special $\Delta s$,
Equilateral $\Delta s$ s: All 4 points are located at the same point.

Isosceles $\Delta s$ : All 4 points are collinear.

